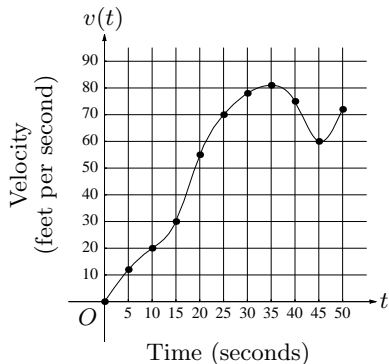


1998 Calculus AB Scoring Guidelines



$t$ (seconds)	$v(t)$ (feet per second)
0	0
5	12
10	20
15	30
20	55
25	70
30	78
35	81
40	75
45	60
50	72

3. The graph of the velocity  $v(t)$ , in ft/sec, of a car traveling on a straight road, for  $0 \leq t \leq 50$ , is shown above. A table of values for  $v(t)$ , at 5 second intervals of time  $t$ , is shown to the right of the graph.
- During what intervals of time is the acceleration of the car positive? Give a reason for your answer.
  - Find the average acceleration of the car, in  $\text{ft/sec}^2$ , over the interval  $0 \leq t \leq 50$ .
  - Find one approximation for the acceleration of the car, in  $\text{ft/sec}^2$ , at  $t = 40$ . Show the computations you used to arrive at your answer.
  - Approximate  $\int_0^{50} v(t) dt$  with a Riemann sum, using the midpoints of five subintervals of equal length. Using correct units, explain the meaning of this integral.

- (a) Acceleration is positive on  $(0, 35)$  and  $(45, 50)$  because the velocity  $v(t)$  is increasing on  $[0, 35]$  and  $[45, 50]$

3 { 1: (0, 35)  
1: (45, 50)  
1: reason

Note: ignore inclusion of endpoints

- (b) Avg. Acc. =  $\frac{v(50) - v(0)}{50 - 0} = \frac{72 - 0}{50} = \frac{72}{50}$   
or 1.44  $\text{ft/sec}^2$

1: answer

- (c) Difference quotient; e.g.  
 $\frac{v(45) - v(40)}{5} = \frac{60 - 75}{5} = -3 \text{ ft/sec}^2$  or  
 $\frac{v(40) - v(35)}{5} = \frac{75 - 81}{5} = -\frac{6}{5} \text{ ft/sec}^2$  or  
 $\frac{v(45) - v(35)}{10} = \frac{60 - 81}{10} = -\frac{21}{10} \text{ ft/sec}^2$

2 { 1: method  
1: answer

Note: 0/2 if first point not earned

-or-

Slope of tangent line, e.g.  
through  $(35, 90)$  and  $(40, 75)$ :  $\frac{90 - 75}{35 - 40} = -3 \text{ ft/sec}^2$

- (d)  $\int_0^{50} v(t) dt$   
 $\approx 10[v(5) + v(15) + v(25) + v(35) + v(45)]$   
 $= 10(12 + 30 + 70 + 81 + 60)$   
 $= 2530 \text{ feet}$

3 { 1: midpoint Riemann sum  
1: answer  
1: meaning of integral

This integral is the total distance traveled in feet over the time 0 to 50 seconds.