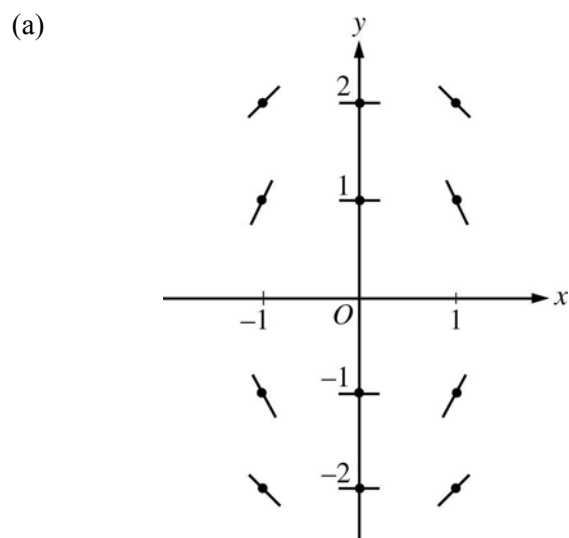
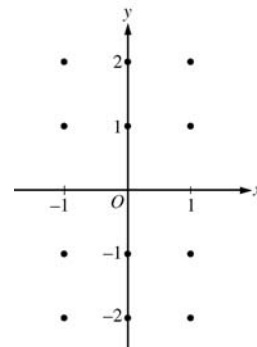


**AP<sup>®</sup> CALCULUS AB  
2005 SCORING GUIDELINES**

**Question 6**

Consider the differential equation  $\frac{dy}{dx} = -\frac{2x}{y}$ .

- (a) On the axes provided, sketch a slope field for the given differential equation at the twelve points indicated.  
**(Note: Use the axes provided in the pink test booklet.)**
- (b) Let  $y = f(x)$  be the particular solution to the differential equation with the initial condition  $f(1) = -1$ . Write an equation for the line tangent to the graph of  $f$  at  $(1, -1)$  and use it to approximate  $f(1.1)$ .
- (c) Find the particular solution  $y = f(x)$  to the given differential equation with the initial condition  $f(1) = -1$ .



- (b) The line tangent to  $f$  at  $(1, -1)$  is  $y + 1 = 2(x - 1)$ .  
Thus,  $f(1.1)$  is approximately  $-0.8$ .

- (c)  $\frac{dy}{dx} = -\frac{2x}{y}$   
 $y \, dy = -2x \, dx$   
 $\frac{y^2}{2} = -x^2 + C$   
 $\frac{1}{2} = -1 + C; C = \frac{3}{2}$   
 $y^2 = -2x^2 + 3$   
 Since the particular solution goes through  $(1, -1)$ ,  
 $y$  must be negative.  
 Thus the particular solution is  $y = -\sqrt{3 - 2x^2}$ .

2 :  $\begin{cases} 1 : \text{zero slopes} \\ 1 : \text{nonzero slopes} \end{cases}$

2 :  $\begin{cases} 1 : \text{equation of the tangent line} \\ 1 : \text{approximation for } f(1.1) \end{cases}$

5 :  $\begin{cases} 1 : \text{separates variables} \\ 1 : \text{antiderivatives} \\ 1 : \text{constant of integration} \\ 1 : \text{uses initial condition} \\ 1 : \text{solves for } y \end{cases}$

Note: max 2/5 [1-1-0-0-0] if no constant of integration  
 Note: 0/5 if no separation of variables