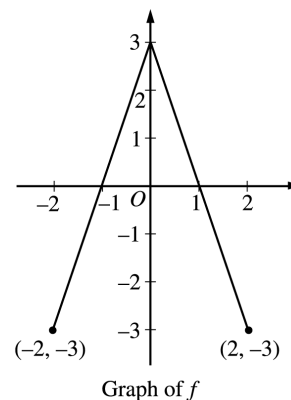


# AP<sup>®</sup> CALCULUS AB 2002 SCORING GUIDELINES

## Question 4

The graph of the function  $f$  shown above consists of two line segments. Let  $g$  be the function given by  $g(x) = \int_0^x f(t) dt$ .



- (a) Find  $g(-1)$ ,  $g'(-1)$ , and  $g''(-1)$ .
- (b) For what values of  $x$  in the open interval  $(-2, 2)$  is  $g$  increasing? Explain your reasoning.
- (c) For what values of  $x$  in the open interval  $(-2, 2)$  is the graph of  $g$  concave down? Explain your reasoning.
- (d) On the axes provided, sketch the graph of  $g$  on the closed interval  $[-2, 2]$ .

(a)  $g(-1) = \int_0^{-1} f(t) dt = -\int_{-1}^0 f(t) dt = -\frac{3}{2}$   
 $g'(-1) = f(-1) = 0$   
 $g''(-1) = f'(-1) = 3$

$$3 \left\{ \begin{array}{l} 1 : g(-1) \\ 1 : g'(-1) \\ 1 : g''(-1) \end{array} \right.$$

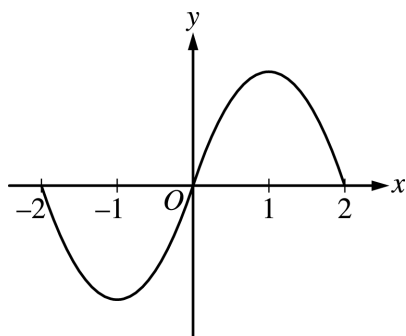
(b)  $g$  is increasing on  $-1 < x < 1$  because  $g'(x) = f(x) > 0$  on this interval.

$$2 \left\{ \begin{array}{l} 1 : \text{interval} \\ 1 : \text{reason} \end{array} \right.$$

(c) The graph of  $g$  is concave down on  $0 < x < 2$  because  $g''(x) = f'(x) < 0$  on this interval.  
 or  
 because  $g'(x) = f(x)$  is decreasing on this interval.

$$2 \left\{ \begin{array}{l} 1 : \text{interval} \\ 1 : \text{reason} \end{array} \right.$$

(d)



$$2 \left\{ \begin{array}{l} 1 : g(-2) = g(0) = g(2) = 0 \\ 1 : \text{appropriate increasing/decreasing} \\ \text{and concavity behavior} \\ < -1 > \text{vertical asymptote} \end{array} \right.$$