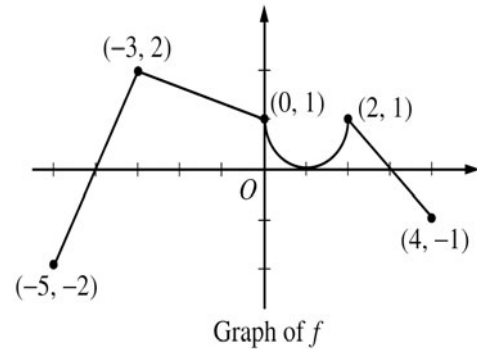


**AP<sup>®</sup> CALCULUS AB  
2004 SCORING GUIDELINES**

**Question 5**

The graph of the function  $f$  shown above consists of a semicircle and three line segments. Let  $g$  be the function given by  $g(x) = \int_{-3}^x f(t) dt$ .



- (a) Find  $g(0)$  and  $g'(0)$ .
- (b) Find all values of  $x$  in the open interval  $(-5, 4)$  at which  $g$  attains a relative maximum. Justify your answer.
- (c) Find the absolute minimum value of  $g$  on the closed interval  $[-5, 4]$ . Justify your answer.
- (d) Find all values of  $x$  in the open interval  $(-5, 4)$  at which the graph of  $g$  has a point of inflection.

(a)  $g(0) = \int_{-3}^0 f(t) dt = \frac{1}{2}(3)(2+1) = \frac{9}{2}$   
 $g'(0) = f(0) = 1$

2 :  $\begin{cases} 1 : g(0) \\ 1 : g'(0) \end{cases}$

- (b)  $g$  has a relative maximum at  $x = 3$ .  
 This is the only  $x$ -value where  $g' = f$  changes from positive to negative.

2 :  $\begin{cases} 1 : x = 3 \\ 1 : \text{justification} \end{cases}$

- (c) The only  $x$ -value where  $f$  changes from negative to positive is  $x = -4$ . The other candidates for the location of the absolute minimum value are the endpoints.

3 :  $\begin{cases} 1 : \text{identifies } x = -4 \text{ as a candidate} \\ 1 : g(-4) = -1 \\ 1 : \text{justification and answer} \end{cases}$

$$g(-5) = 0$$

$$g(-4) = \int_{-3}^{-4} f(t) dt = -1$$

$$g(4) = \frac{9}{2} + \left(2 - \frac{\pi}{2}\right) = \frac{13 - \pi}{2}$$

So the absolute minimum value of  $g$  is  $-1$ .

- (d)  $x = -3, 1, 2$

2 : correct values  
 $\langle -1 \rangle$  each missing or extra value